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# APPLIED FIELD DEPENDENCES OF LOCAL MAGNETIC FIELDS IN SINGLE $\text{Fe}_3\text{O}_4$ CRYSTALS

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## **Applied Field Dependences of Local Magnetic Fields in Single Fe<sub>3</sub>O<sub>4</sub> Crystals**

### **Synopsis:**

The internal fields in single crystals of magnetite (Fe<sub>3</sub>O<sub>4</sub>) have been previously studied through muon-spin rotation ( $\mu$ SR). By Maximum-Entropy (ME)  $\mu$ SR, [2] we have analyzed  $\mu$ SR Fe<sub>3</sub>O<sub>4</sub> data with external field parallel to the  $\langle 111 \rangle$ ,  $\langle 110 \rangle$  or  $\langle 100 \rangle$  axis. Our ME $\mu$ SR field-dependent studies lead to a better understanding of the local magnetism and conduction mechanism in this Mott-Wigner glass.

## **Applied field dependences of local magnetic fields**

### **in single Fe<sub>3</sub>O<sub>4</sub> crystals: a Maximum-Entropy $\mu$ SR study.**

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**Abstract** The internal fields in single crystals of magnetite (Fe<sub>3</sub>O<sub>4</sub>) have been previously studied through muon-spin rotation ( $\mu$ SR). By Maximum-Entropy (MaxEnt, ME)  $\mu$ SR, we have analyzed  $\mu$ SR data of single crystals of Fe<sub>3</sub>O<sub>4</sub> with external fields parallel to the <111>, <110> or <100> axis. Several  $\mu$ SR time series indicate a beat pattern. By curve fitting and confirmed with improved precision by ME $\mu$ SR second frequency signals are seen in the temperature range above the Verwey transition ( $T_V = \sim 123$  K). Assuming one demagnetization field and one muon-probe-site set, we find for roomtemperature (RT) <111> Fe<sub>3</sub>O<sub>4</sub> fields close to the maximum allowable. For <110> at RT Fe<sub>3</sub>O<sub>4</sub>, indicates a second  $\mu$ SR signal is seen. We compare our RT field-dependent results with those observed for 205 K <110> Fe<sub>3</sub>O<sub>4</sub> to study a 2nd order phase transition observed at the Wigner temperature  $T_W$  (about twice  $T_V$ ). The existence of these secondary signals may be related to phonon-assisted 3d-electron hopping. Another possibility could be the existence of magnetically different muon-probe sites. Our ME $\mu$ SR field-dependent studies lead to a better understanding of the local magnetism and conduction mechanism in this Mott-Wigner glass.

## 1. Introduction

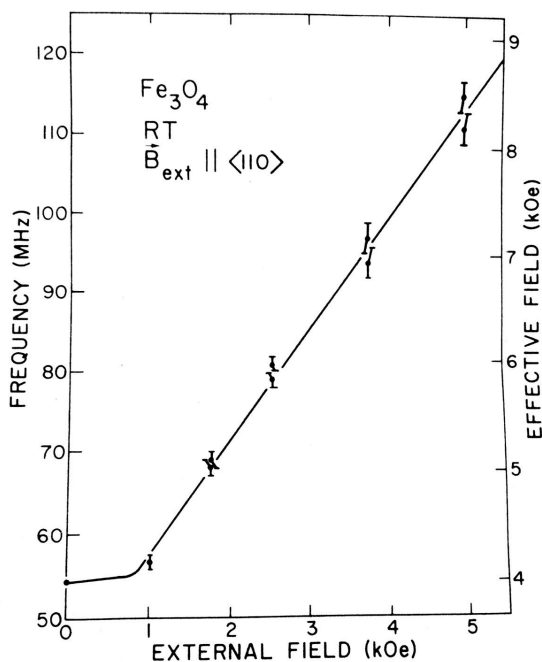
Magnetite ( $\text{Fe}_3\text{O}_4$ ) is a ferrimagnetic oxide.  $\text{Fe}_3\text{O}_4$  has a fully spin-polarized band, making an ideal compound for studying basic spintronics. At the Verwey temperature ( $T_V \sim 123$  K)  $\text{Fe}_3\text{O}_4$  shows a semimetal-to-insulator transition, which is related to the properties of the “extra 3d” ( $3d^*$ ) electrons. The Verwey transition is a first order transition.[1-2] The Wannier states for these  $3d^*$  conduction electrons in  $\text{Fe}_3\text{O}_4$  indicate a mixture of localized and delocalized electron/hole states [3-4]. Magnetic anomalies, observed between  $T_V$  and the Wigner temperature ( $T_W \approx 247$  K), show  $\text{Fe}_3\text{O}_4$  can be considered a Wigner electron glass [5]. The resistivity is a minimum at  $T_W$  suggesting glassy, precursor effects in the  $T_V - T_W$  region.

Magnetite’s physical-chemical formula reads:  $(\text{Fe}^{3+})_A [\text{Fe}_2^{3+} \text{e}^{-1}]_B \text{O}_4^{2-}$ . The Fe ions have two different configurations: in the tetrahedral site (A) the  $\text{Fe}^{3+}$  ion is surrounded by four  $\text{O}^{2-}$  ions, while in the octahedral site (B) the  $\text{Fe}^{3+/2+}$  ion is surrounded by six  $\text{O}^{2-}$  ions [6-7]. The electron configuration of  $(\text{Fe}^{3+})_A$  is  $3d^5$  and all 5 spins are parallel. These spins on the A sublattice are antiparallel to those on the B sublattice; the  $3d^*$  electron has a spin-down orientation ( $\downarrow \text{e}^{-1}$ ).

The Magneto-chemical formula is:  $(\downarrow \text{Fe}^{3+})_A [\uparrow \text{Fe}_2^{3+} \downarrow \text{e}^{-1}]_B \text{O}_4^{2-}$ . The top energy band is half filled by  $3d^*$  electrons, which are fully spin polarized. Our studies support the phonon-assisted electron-spin hopping model and the Mott-Wigner glass description of  $\text{Fe}_3\text{O}_4$ . [5]

## 2. Previous $\mu$ SR studies, using Fourier Transformation and Curve Fitting

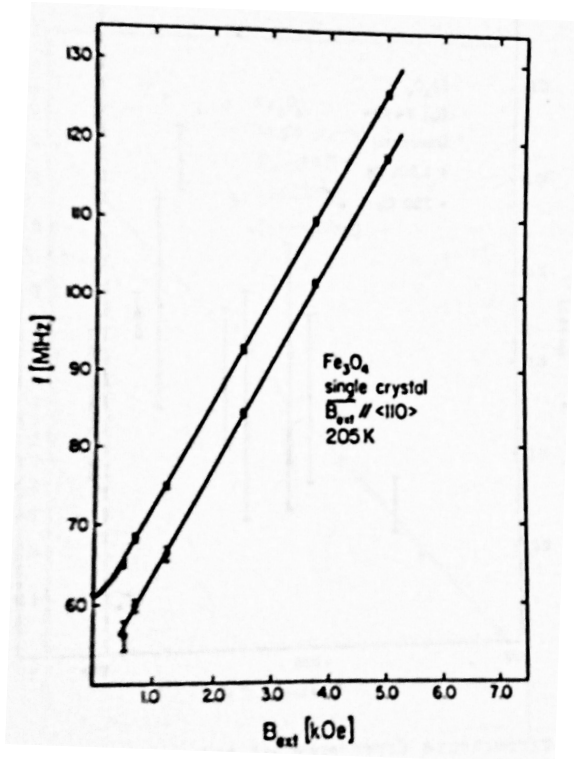
Previous  $\mu$ SR studies [5, 8] studied the behavior of the internal magnetic field in  $\text{Fe}_3\text{O}_4$  as a function of temperature and external field  $B_{\text{ext}}$ . These studies showed that at  $T_w$  there appears to be a 2nd order phase transition. Further, the local field  $B_{\text{loc}}$  can be approximated by  $B_{\text{loc}} = B_{\text{ext}} - B_{\text{dem}}$  for  $B > B_{\text{dem}}$  and  $B_{\text{loc}} = B_{\text{loc}}(\text{ZF})$  for  $B < B_{\text{dem}}$ .  $B_{\text{dem}}$  is the demagnetization field. For the  $\langle 111 \rangle$  orientation at room temperature (RT) the external field dependence results indicated a field somewhat larger than the theoretical maximum allowed. These studies were done using Fourier transformation (FT) and curve fitting (CF). The CF results gave only a reasonable frequency values, with large error bars for its amplitudes and relaxation rates. A field dependency was observed for  $\text{Fe}_3\text{O}_4$  at RT in the  $\langle 110 \rangle$  orientation. See Fig 1. This trend differs from the one observed at 205 K at  $\langle 110 \rangle$  orientation. See Fig 2.



**Figure 1:** External field dependence observed for  $B // \langle 110 \rangle$  magnetite at RT. The frequencies

observed follow the expected linear trend with a slope of 13.55 MHz/kOe and  $B_{\text{dem}} = \sim 0.9$  kOe.

At 5 kOe, the highest field is somewhat larger than theoretically allowed.



**Figure 2.** Observed  $\mu$ SR frequencies with  $B // \langle 110 \rangle$ . At 205 K the two frequency signals clearly follow the expected linear trend with a slope of 13.55 MHz/kOe with both a  $B_{\text{dem}}$  of about 0.5 kOe. The lower frequency signal at zero field has not been seen by FT and CF analysis. At zero field, FT & CF studies [5, 8] indicated only one frequency signal.

### 3.0 MaxEnt- $\mu$ SR $\text{Fe}_3\text{O}_4$ in progress

Our MaxEnt [8-10] study analyzes original  $\text{Fe}_3\text{O}_4$   $\mu$ SR data to investigate these  $T_V$  &  $T_W$

transitions and potential precursor effects in the  $T_V - T_W$  region. For more detail on our MaxEnt-Burg technique applied to  $\mu$ SR, see the Appendix.

### 3.1 ME $\mu$ SR $\text{Fe}_3\text{O}_4$ $B // \langle 111 \rangle$ field dependence

The field-dependent  $\mu$ SR data of  $B // \langle 111 \rangle$   $\text{Fe}_3\text{O}_4$  at RT have been analyzed using MaxEnt. A filter time  $T_f$  of 0.6  $\mu$ s is found to be about twice the relaxation time of the frequency signal.

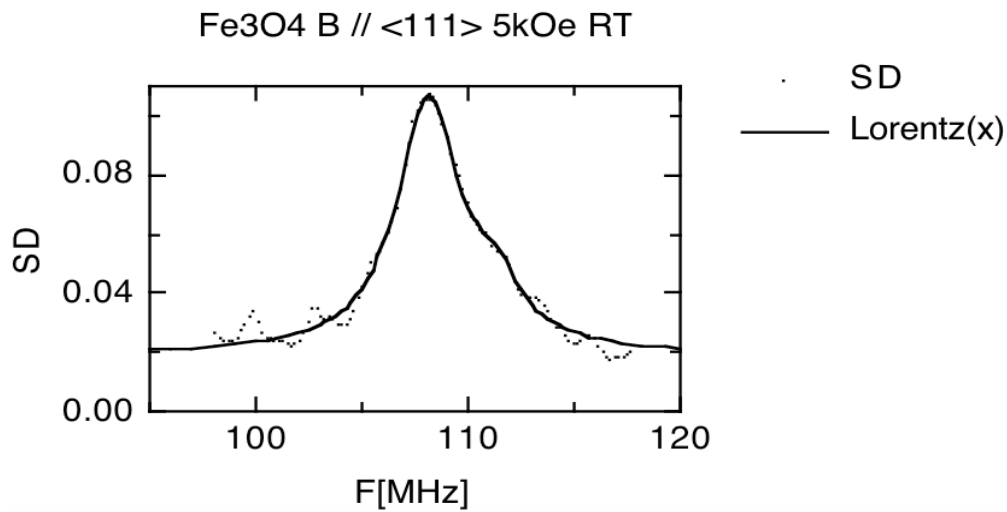
The ME $\mu$ SR  $\langle 111 \rangle$   $\text{Fe}_3\text{O}_4$  results are consistent with, yet are more precise than the CF results.

[5, 8] In Fig 3, we show the  $\langle 111 \rangle$  ME transform at 5 kOe, RT fitted with two Lorentzians (Lor)

that describes the asymmetric broad peak best. A fit with two Gaussians (Gau) or a Gau/Lor combination gave a higher  $\chi^2$ . In Table 1 below, our fit results are given. The fact that the Lor fits are better implicates exponential  $\mu$ -spin relaxation, caused by the muons moving among the  $\mu$ -O sites within the empty O octahedrons at RT. [8, 10]

Note, for a perfect alignment  $B // \langle 111 \rangle$  the six muon-stop sites within an empty O-octahedron are magnetically and electrically equivalent, due to rotation symmetry around the  $\langle 111 \rangle$  axis.

Assuming one  $\mu$ -site and one  $B_{\text{dem}}$ , the highest 111-MHz frequency is about the maximum allowable. [5, 8] A slight misalignment of the  $B // \langle 111 \rangle$  alignment causes the  $\mu$ -O sites to be magnetically different, resulting in an asymmetric ME distribution.



**Figure 3.** Spectral density for  $B \langle 111 \rangle$  Fe<sub>3</sub>O<sub>4</sub> at 5kOe, RT, with a best fit of 2 Lorentzians.

**Table 1:** Fit parameters for B // <111> RT MaxEnt transform. The two Lorentzians give the best fit parameters and lowest  $\chi^2$ . S in MHz & K in  $\text{MHz}^{-1}$ . The substantial  $\chi^2$  reduction for two Lor\*s is caused by a much better fit for the 105 – 110 MHz interval, than that for two Gau\*s.

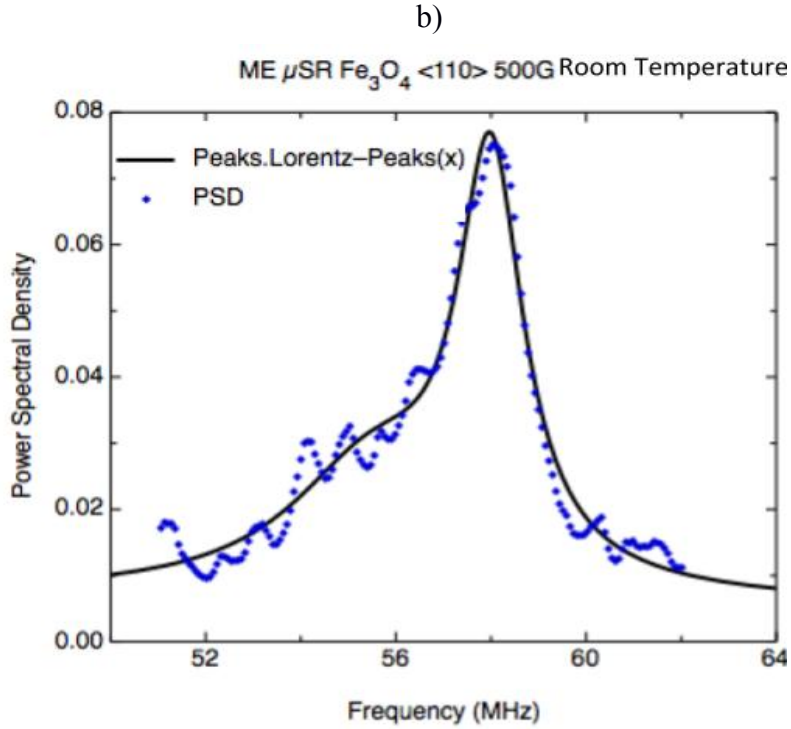
Fit $f^*$	$\chi^2 * 10^3$	ME-BG	A	S / K	f [MHz]
Gaussian	2.54	.026(1)	.182(3)	4.1(2) MHz	108.41(5)
2 Gau	1.31	.025(1)	.193(3)	2.7(2)	108.1(1)
			.045(5)	1.5(5)	111.9(2)
Lorentzian	1.75	.018(1)	.089(2)	.20(1) $\text{MHz}^{-1}$	108.34(2)
2 Lor	1.00	.019(1)	.085(2)	.30(2)	108.13(4)
			.016(2)	.5(2)	111.3(2)

### 3.2 ME $\mu$ SR Fe<sub>3</sub>O<sub>4</sub> External Field in <110> orientation

#### 3.2.1 ME $\mu$ SR Fe<sub>3</sub>O<sub>4</sub> B // <110> RT

We have evaluated MaxEnt transforms for low external fields for B // <111> & RT. As a zero approximation for  $T_f$ , a 1 $\mu$ s filter time is used. At zero field, we find only one peak of 54.4 MHz. The ME $\mu$ SR transforms for 500 Oe indicate a second signal. A two-Lorentzian fit reveals two peaks at 55.5 MHz and 59.0 MHz. See Fig 4. If  $B_{\text{dem}}$  is much less than 500 Oe, then we expect for f(high) about 61 MHz. The f(low) peak indicates a magnetically different set of muon sites, as B // <110>.





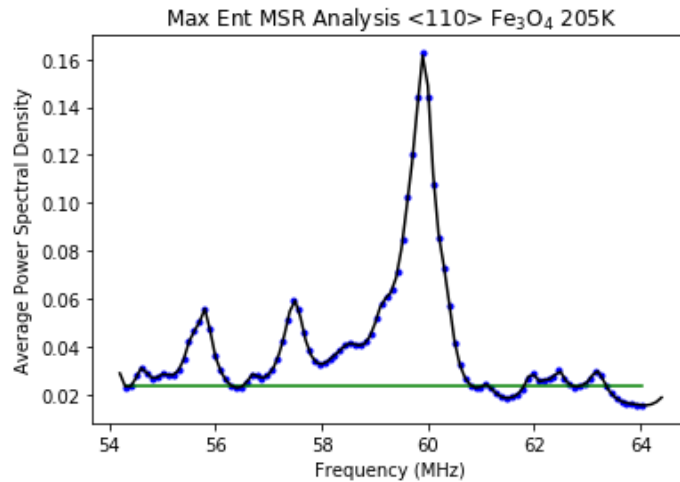
**Figure 4:** A two-Lor fit is shown in the ME $\mu$ SR transform ( $T_f = 1\mu\text{s}$ )

for B (500-Oe) //  $\langle 110 \rangle$   $\text{Fe}_3\text{O}_4$

### 3.2.2 ME $\mu$ SR $\text{Fe}_3\text{O}_4$ B // $\langle 110 \rangle$ 205 K

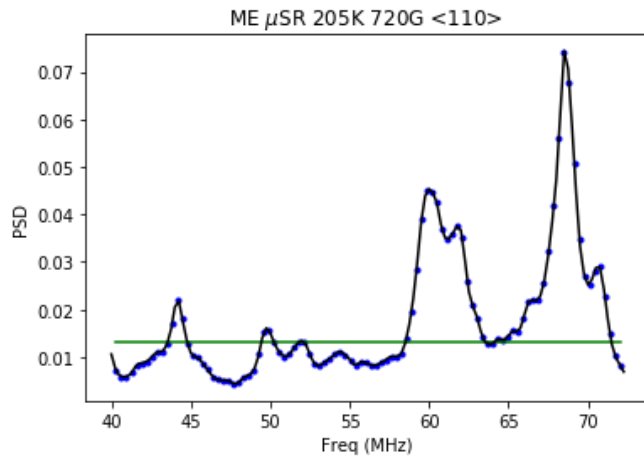
In Fig 5 ME $\mu$ SR tranforms for B //  $\langle 110 \rangle$  B = 100 Oe and T = 205 K is displayed. With an optimized signal ( $T_f = 1\mu\text{s}$ ) the distribution indicates two smaller signals (55 & 57 MHz) besides the main signal at 60 MHz. This is different behavior than observed at RT and 500 Oe (Fig 4).

The 55 & 57 -MHz signals were not seen in CF analysis – see also Fig 2.



**Figure 5.** ME $\mu$ SR transform ( $T_f = 1 \mu\text{s}$ ) for B (100 Oe) // <110> Fe<sub>3</sub>O<sub>4</sub> at 205 K. The curve is an interpolation to guide the eye; the line is an estimate for the ME background.

In Fig 6 ME $\mu$ SR transform is shown for B // 720 Oe,  $T = 205 \text{ K}$ ,  $T_f = 0.5 \mu\text{s}$ . Besides the peak at 68 MHz, a second signal is seen at 60 MHz, possibly split as also the 100-Oe transform (Fig 5) indicates. The frequency difference between the two signals is about 8 MHz which is about equal to the observed frequency shifts seen at  $T_V$  and at  $T_W$  in zero field. [5, 8] This suggests that in the  $T_V - T_W$  region, two magnetically different subregions in the B sublattice exists: one following the normal magnetization curve, and one for which a Verwey-like structure and phase transition has been induced by the applied field. This may well be glassy, precursor effects.



**Figure 6.** ME $\mu$ SR transform ( $T_f = 0.5 \mu\text{s}$ ) for B (720 Oe) // <110> at 205 K. The curve is an interpolation to guide the eye; the line is an estimate for the ME background

### 3.3 ME $\mu$ SR Fe<sub>3</sub>O<sub>4</sub> B // <100> orientation field dependence.

We have evaluated the ME $\mu$ SR results in Fe<sub>3</sub>O<sub>4</sub> for B // <100> for small fields. These RT transforms for B// <100> orientation indicate no substantial change up to 1 kOe. Only one peak signal at zero field, 50 Oe and 1 kOe is seen. The fitted frequencies of about 55 MHz are independent of  $B \leq 1 \text{ kOe}$ , suggesting for B//<100>  $B_{\text{dem}}$  is larger than 1 kOe.

#### **4. Conclusive Remarks**

Using ME $\mu$ SR, we find with improved precision the local magnetic fields in Fe<sub>3</sub>O<sub>4</sub> crystals.

Observation of two signals close in frequency is consistent with the beat patterns seen in the  $\mu$ SR time series.

We have observed two frequencies for the  $\langle 111 \rangle$  orientation at 5 kOe, RT; the smaller signal indicates a slight misalignment of the  $\langle 111 \rangle$  Fe<sub>3</sub>O<sub>4</sub> crystal.

For the  $\langle 110 \rangle$  orientation, a second signal is observed. These B-dependent  $\mu$ SR signals indicate a much different behavior at RT than they do at 205 K. The  $\mu$ SR signals at 205 K suggest a splitting in the magnetization, plausibly caused by glassy precursor effects above  $T_V$ .

Thus Fe<sub>3</sub>O<sub>4</sub> is more like a narrow-band (degenerate) semiconductor than a semimetal.

3d\* electrons appear to be important ingredients of the conduction mechanism in Fe<sub>3</sub>O<sub>4</sub>, supporting the phonon-assisted electron hopping model. [5,8]

#### **Acknowledgements**

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## *Appendix*

### *MaxEnt Muon-Spin Research*

Muon-Spin Rotation ( $\mu$ SR) is a magnetic resonance technique, in which an implanted positive muon ( $\mu^+$ ) act as a magnetic probe. To measure the local magnetic fields in  $\text{Fe}_3\text{O}_4$ , we use  $\mu$ SR. The muon-decay distribution [a, b] is described by:

$$N(t) = N_0 e^{-t/\tau} [1 + S(t)] + BG$$

where  $N(t)$  is the number of muons decayed at time  $t$ ,  $N_0$  the initial muon-decay events at  $t = 0$ ,  $\tau$  the muon-decay time of 2.2  $\mu$ s,  $S(t)$  the oscillatory signal and  $BG$  the background noise. The time histogram of the muon-decay events shows the Larmor muon-spin precession superimposed on the exponential muon decay [a, b]. The observed frequencies in  $S(t)$  are proportional to the magnetic fields.

These  $\mu^+$  probes bond with  $\text{O}^{2-}$  ions at  $\sim 0.1$  nm away from the O-ion. For  $\text{Fe}_3\text{O}_4$ , our preliminary calculations indicate, there are six equivalent muon-stop sites located in an empty oxygen octahedron between the A and B sites. Electrically, these sites are all equivalent.

### **Maximum Entropy (MaxEnt, ME)**

The muon-spin polarization and time series  $S(t)$  can be transformed into a frequency domain to find the magnetic field distribution. To reduce Poisson noise, we optimize the ME signal-to-noise ratio by varying  $T_f$  the filter time. [a] On average, we've found  $T_f$  is about twice the 'lifetime' of the  $\mu$ SR signal.

MaxEnt is an advantageous method that produces sharper signals in a frequency transform, while reducing noise and eliminating sinc wiggles, commonly seen in Fourier analysis. Also, for weak and/or broad signals, Fourier analysis and curve fitting are less effective.

The MaxEnt-Burg technique is an auto-regressive method that assumes a correlation between the muon-spin signal,  $S(i)$  at any time  $i$ , and previous times,  $S(i-k)$  [a]. The Burg algorithm assumes each data point for  $S(i)$  can be expressed as:

$$S(i) = \sum_{k=1}^p S(i-k)c_k + n_i$$

The optimal number of auto-regression coefficients ( $p$ ) lies between  $N/3$  and  $N/5$ , where  $N$  represents the number of data points [a]. The MaxEnt transformation or spectral density is obtained by taking the square root of the power of the spectral density,  $P(f)$  given by:

$$P(f) = \frac{2\sigma^2}{\left|1 - \sum_{k=1}^p c_k e^{-2\pi i k f}\right|^2}$$

The  $\mu$ SR signal provides information about the frequency distribution. The spectral density or the frequency distribution is a direct measure of the local magnetic field distribution.

Muon-spin rotation in conjunction with Maximum Entropy technique is a sensitive tool [a] to search for the predicted (weak) magnetic effects. MaxEnt  $\mu$ SR has been proven useful for probing magnetism in cuprates by: (1) indicating d-wave symmetry for cuprate superconductivity, and (2) pointing toward extra condensate near the CuO-chain layers of  $\text{RBa}_2\text{Cu}_3\text{O}_{7-\delta}$  (RBCO) below about  $T_c/3$ . [b]

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